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Explaining stability of transition metal carbides – and why TcC does not exist

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Abstract

We analyze the formation of transition metal (TM) carbides, as being determined by the strength of TM-TM and TM-C bonds, as well as lattice distortions induced by C interstitials. With increasing fillings of the d-band of TMs, TM-C bonds become increasingly weaker from left of the Periodic Table to right, with lesser and lesser C atoms entering the TMs lattice. Technetium (Tc) turns out to be a critical point for the formation of carbides, guiding us to resolve a long-standing dispute. The predicted Tc carbides, agreeing with measured X-ray absorption spectra, should decompose to cubic Tc and graphite above 2000 K. Consequently, we show that what has been claimed as TcC (with rocksalt structure) is actually a high-temperature cubic phase of elemental technetium.

Keywords transition metal carbide, Tc, Tc carbide, evolutionary algorithms, crystal structure prediction, X-ray absorption spectra.

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Transition metal carbides (TM$_x$C$_y$, $x \geq y$) have attracted increasing attention due to their “platinum-like” electronic structures, hardness, high melting temperature, and good thermal and electrical conductivities 1-6. Due to these properties, TM$_x$C$_y$ compounds are not only advanced materials that can be applied in extreme environments, but also a most promising kind of low-cost catalysts. Mo carbides are used as catalysts for hydrogen production reactions 7, 8, but the activities of γ-MoC and β-Mo$_2$C are different 9. Detailed knowledge of TM$_x$C$_y$ compounds is the key for related material designs, but the field is marked by many controversies. For example, Wang et al. suggested the synthesis of CrC 10, but some other researchers thought it was impossible 11. To guide studies in future, it is important to know the formation mechanism of TM$_x$C$_y$ compounds, i.e., which compounds are possible, and why.

Groups IVB and VB TM$_x$C$_y$ compounds usually are monocarbides with NaCl structure (TiC, ZrC, HfC, VC, NbC and TaC), while compounds of group VIB TM$_x$C$_y$ are Mo$_2$C, W$_2$C and WC 2. Further increasing fillings of d-band (i.e., for TMs at the right side of the Periodic Table), only TM-rich carbides were obtained, e.g., Fe$_3$C 12. Consistent with nonstoichiometry, TM$_2$C, TM$_4$C$_3$, TM$_3$C$_2$, TM$_6$C$_5$, and TM$_8$C$_7$ superstructures may form, and their structures were predicted recently 13, 14. Indeed, Ta$_6$C$_5$, Ta$_2$C, Ta$_4$C$_3$, Ta$_3$C$_2$, Hf$_2$C$_2$, and Hf$_6$C$_5$ were found to be thermodynamically stable for Ta-C 15 and Hf-C 6 systems, respectively, with the help of the evolutionary algorithm USPEX 16, 17. Although it is possible to make detailed and reliable numerical predictions, a general understanding of the formation of TM$_x$C$_y$ compounds is still lacking.

The trend of stability for transition metal carbides We can consider C atoms in TM$_x$C$_y$ compounds as interstitials in the TM-sublattice. As a result of inserting carbon atoms, TM-TM bonds are weakened, but this is compensated by the formation of TM-C bonds. Stability of carbides depends on the detailed balance between these factors. As reported 18, nobleness increases from left to right for 3d, 4d and 5d TMs. Corresponding TM-C bonds should become weaker and weaker, and thus lesser and lesser C atoms could enter the TMs lattice. Therefore, C content in TM$_x$C$_y$ compounds, per TM atom, should decrease from left to right for TMs in the Periodic Table.
The strength of TM-TM bonds is revealed by the cohesive energy of a TM (E_{Coh}), which is computed as

$$E_{Coh} = -\left( \frac{1}{n} E_{TM}^{bulk} - E_{TM}^{atom} \right),$$

(1)

where $\frac{1}{n} E_{TM}^{bulk}$ is the total energy of a TM normalized per atom, and $E_{TM}^{atom}$ is the total energy of an isolated TM atom. As seen in Fig.1, $E_{Coh}$ values do not monotonically change, especially for 3d TMs.

![Fig.1 Cohesive energies of TMs (E_{coh}), C dissolution energies calculated using TM_{16}C model (E_{C-dis}), formation energies of TM monocarbides (E_{TMC}), and charges captured by C atoms in TM monocarbides (ΔC_{cag}). NaCl- or WC-type TM monocarbides are selected in the light of E_{C-dis} values.](image)

At low C contents, the strength of TM-C bonds is estimated by a TM_{16}C model. The C dissolution energy (E_{C-dis}) is defined as

$$E_{C-dis} = E_{TM_{16}C} - E_{TM_{16}}^{bulk} - \frac{1}{m} E_{(graphite)},$$

(2)

where $E_{TM_{16}}^{bulk}$ and $E_{TM_{16}C}$ are total energies of TM and TM_{16}C, respectively. $\frac{1}{m} E_{(graphite)}$ is the total energy of graphite normalized per atom. Negative (positive) $E_{C-dis}$ values mean that C atoms would (would not) like to occupy octahedral sites.

Except for group VIB TMs, $E_{C-dis}$ values decrease from left to right (Fig.1).

In MoC and WC, carbon atoms occupy trigonal prismatic sites, corresponding
to positive $E_{\text{C-dis}}$ values. In contrast, C atoms in TiC, ZrC, HfC, VC, NbC and TaC occupy octahedral sites and have negative $E_{\text{C-dis}}$ values. At a high C content, the strength of TM-C bonds is estimated by NaCl- or WC-type TM monocarbide, which could be chosen according to $E_{\text{C-dis}}$ values. The formation energy of a TM monocarbide is defined as

$$E_{\text{TMC}} = E_{\text{bulk}}^{\text{TMC}} - \frac{1}{n} E_{\text{TM}}^{\text{bulk}} - \frac{1}{m} E(\text{graphite}),$$

(3)

where $E_{\text{bulk}}^{\text{TMC}}$ is the total energy of a certain TM monocarbide. Negative $E_{\text{TMC}}$ values indicate that monocarbides are thermodynamically stable.

Charge transfer contributes to the strength of TM-C bonds of TM$_x$C$_y$ compounds, whose definition is

$$\Delta C_{\text{chg}} = C_{\text{chg}}(\text{TMC}) - C_{\text{chg}}(\text{graphite}),$$

(4)

where $C_{\text{chg}}(\text{TMC})$ and $C_{\text{chg}}(\text{graphite})$ are Bader charges of a C atom in a TM monocarbide and in graphite, respectively. Bader analysis was performed using grid-based algorithm. In Fig.1, $\Delta C_{\text{chg}}$ values are larger for TMs at the left side of the Periodic Table, indicating that there TM-C bonds are stronger. In agreement with this tendency, a theoretical calculation indicates that the formation of a C vacancy in ZrC costs 58 mRy at 0 K, and it is more difficult than that in NbC (42 mRy).

Negative $E_{\text{C-dis}}$ values correlate with $E_{\text{TMC}}$ for NaCl-type monocarbides, since their local structure is similar. $E_{\text{TMC}}$ values are -1.62, -1.63, -1.88, -0.83, -1.06 and -1.17 eV for TiC, ZrC, HfC, VC, NbC and TaC, respectively, showing a strong thermodynamic driving force for their formation. For elements forming WC-type monocarbides, $E_{\text{C-dis}}$ values turn out to be positive: 1.65 and 1.99 eV for Mo$_{16}$C and W$_{16}$C, respectively, and $E_{\text{TMC}}$ values are -0.18 and -0.24 eV for MoC and WC, respectively, again consistent with their observed formation.

The COOP (Crystal Orbital Overlap Population) analysis reveals that the covalency of Fe- and Mn-C bonds is not as strong as that of Mo-C and W-C bonds.
FeC and MnC are unstable according to their positive $E_{\text{TMC}}$ values, and one could conclude that strong covalency of TM-C bonds is essential for the formation of WC-type monocarbides. At reduced C contents, Fe- and Mn-rich carbides become stable (stressed by the green box) due to the reduced distortion of TMs lattice. Through the same mechanism, TM-rich carbides of group IVB TMs are also stable at lower C contents, e.g., Hf$_3$C$_2$ and Hf$_6$C$_5$ \(^6\), although stoichiometric HfC is also stable.

$E_{\text{TMC}}$ values of WC-type RuC and OsC are 0.51 and 1.84 eV, respectively, implying their instability. Ru and Os are more inert (noble), since their d-band fillings are larger \(^8\). Positive $E_{\text{C-dis}}$ values for Ru$_{16}$C (1.70 eV) and Os$_{16}$C (2.85 eV) further manifest the nobleness of Ru and Os, i.e., no carbides form even at low concentrations of carbon. Hypothetical, but now clearly impossible, OsC and RuC were considered as superhard materials \(^4,22\). In the same group of the Periodic Table, Fe-rich carbides (e.g., Fe$_3$C \(^12\)) are stable because the $E_{\text{Coh}}$ value (5.03 eV) of Fe is smaller than those of Ru (7.86 eV) and Os (8.50 eV). Therefore, the formation of carbides is more favorable for TMs with smaller $E_{\text{Coh}}$ values.

According to TMs nobleness \(^8\), Re-C bonds are stronger than Ru-C and Os-C bonds. Therefore, Re carbides would be more likely to form, yet this factor alone is not strong enough, and our USPEX calculation does not find any stable Re carbide (see Supplementary Materials). To sum up, there are no stable carbides for Re, Ru and Os. In contrast, C atoms could enter Tc lattice according to the $E_{\text{C-dis}}$ value of Tc$_{16}$C (-0.02 eV), but the formation of TcC is impossible because of its positive $E_{\text{TMC}}$ (0.27 eV). Consequently, only Tc-rich carbides may be stable.

**The controversy on technetium carbide** As a spent-fuel waste of $^{235}$U fission, radiotoxic $^{99}$Tc is dangerous due to its growing inventory and environmental mobility \(^23\). This challenge can be treated by Tc transmutation ($^{99}$Tc$\rightarrow^{100}$Tc$\rightarrow^{100}$Ru$\rightarrow^{101}$Ru) \(^24\), but the extraction of pure Tc is quite difficult. Tc carbides are a promising alternative target material \(^25\), whose lattice expansions may alleviate resonance shielding of
thermal neutrons in transmutation. About fifty years ago, it was proposed that TcC is the observed high-temperature cubic phase, and it was accepted both experimentally and theoretically. Yet, that phase was also interpreted as cubic Tc on the basis of nuclear magnetic resonance (NMR) data. Furthermore, a cubic phase is present in samples covering a wide range of C content. To summarize, it is unclear what the observed high-temperature cubic phase is, and this long-standing puzzle is of great scientific and technological significance.

**Theoretical calculations** To resolve the controversy on technetium carbide and check our qualitative trend of stability of TM carbides, we searched for all stable Tc carbides using the USPEX code. Eighty structures (with any compositions between pure Tc and pure C, with up to 20 atoms in the primitive unit cell) were randomly produced in the first generation. Each of the subsequent 59 generations contained 50 structures, of which 30%, 30%, 20%, and 20% were produced by heredity, symmetric random algorithm, softmutation and transmutation operators, respectively. Relaxations of candidate structures were done by the VASP code, for exchange-correlation using the generalized gradient approximation in the Perdew-Burke-Ernzerhof form. Core electrons were treated using the projector-augmented wave method, with the plane-wave kinetic energy cutoff of 700 eV. We used uniform Γ-centered k-points meshes with reciprocal-space resolution of \(2\pi \times 0.05 \text{ Å}^{-1}\). These settings produced well-converged results. Stability of compounds was determined using the thermodynamic convex hull construction, where compounds/structures on the convex hull are stable, and those above the convex hull are metastable. The effects of temperature on the stability of compounds were investigated within the quasiharmonic approximation, using the Phonopy code.

Consistent with the trend of stability of TM carbides, three possible Tc-rich carbides are predicted, which are Tc\(_{10}\)C, Tc\(_8\)C and Tc\(_6\)C. Their crystal structures are given in Supplementary Materials. At 0 K, only Tc\(_8\)C is stable. Actually, Tc-rich carbides with different carbon concentrations have been experimentally obtained. To rationalize the experimental result, we define the formation energy of Tc-rich
carbides normalized per Tc atom,

\[ E_{\text{Tc,C}} = \frac{1}{X} \left( E_{\text{Tc,C}} - xE_{\text{Tc}} - \frac{1}{m} E(\text{graphite}) \right), \]

where \( E_{\text{Tc}} \) and \( E_{\text{Tc,C}} \) are the total energies (per atom) of bulk Tc and Tc\(_x\)C carbide, respectively. \( E_{\text{Tc,C}} \) values increase with C concentrations, i.e., \( E_{\text{Tc,C}}(-0.005 \text{ eV}) < E_{\text{Tc,C}}(-0.015) < E_{\text{Tc,C}}(-0.017 \text{ eV}) \). Driven by the thermodynamics, the formation of Tc carbides depends on C content, and maximally 16.7 at.% C could enter Tc lattice. These results are in agreement with experimental results, where excess carbon was present when C content exceeded 17 at.% \(^{25}\). Thus, the experimental finding, where Tc carbides have different C concentrations \(^{25}\), is rationalized theoretically.

The formation of Tc carbides can be viewed as a process of inserting carbon atoms into Tc lattice, resulting in a lattice expansion. Compared with hcp Tc (14.59 Å\(^3\)), the increments of specific cell volume (normalized per Tc atom) are 4.66%, 5.55% and 7.74% for Tc\(_{10}\)C (15.27 Å\(^3\)), Tc\(_8\)C (15.40 Å\(^3\)) and Tc\(_6\)C (15.72 Å\(^3\)), respectively. The first two specific cell volumes (15.55 and 15.65 Å\(^3\)) measured in the experiment \(^{25}\) are larger than that of Tc\(_8\)C. However, the third measurement (15.75 Å\(^3\)) is in excellent agreement with the specific cell volume of Tc\(_6\)C, and it does not further increase with C content (above 17 at.% \(^{25}\)). These results reveal that the formation of Tc carbides depends on C content, and the maximum C concentration is about 17 at.%,
corresponding to Tc\(_6\)C.

**Experimental investigations** In the light of theoretical prediction, Tc\(_6\)C, having the maximum C concentration, can be easily confirmed experimentally. The synthesis of Tc\(_x\)C microcrystallites was carried out according to the procedure of a previous paper \(^{25}\). The sample with 50 at.% C was less fused and could be destroyed easily, revealing the mixture of carbides and graphite. For X-ray absorption measurements, we powered the sample and homogenized it with BN (10 mg Tc\(_x\)C+C–50 mg BN), and then pressed into a special plastic holder of an ESRF-ROBLE device.

The extended x-ray absorption fine structure (EXAFS) and X-ray absorption near-edge spectra (XANES) of Tc K-edge were measured at the Structural Materials...
Science Station (Russian Research Centre Kurchatov Institute) in a transmission geometry, using a Si(111) monoblock monochromator with a slit and two ionization chambers filled with argon–xenon mixture gas. The EXAFS spectra were extracted using Athena and Artemis programs in IFEFFIT package. The multisphere fitting of normalized EXAFS curves $\chi(k)$ was performed in a photoelectron wavenumber range $k$ 3.0–16.0 Å$^{-1}$, with the $k^3$ weight scheme using the photoelectron phases and scattering amplitudes, calculated by FEFF program.

The amplitudes of Fourier transform of XANES spectra are shown in Fig.2 for the Tc$_x$C sample with 50 at.% C. The XANES data indicate that a Tc atom is surrounded by 12 Tc atoms at a distance of 2.72 Å, corresponding to a close-packed structure.

![Fig.2 XANES spectrum of (a) Tc K-edge, and (b) the first derivative for the Tc$_x$C sample with 50 at.% C](image)

The normalized EXAFS curves are shown in Fig.3. The spectrum of Tc$_x$C sample with 50 at.% C is very similar to the reference spectrum of Tc$_x$C obtained in. These results indicate the identity of carbides in the samples having 17 at.% and 50 at.% C. Combined with predicted Tc carbides and their increments of specific cell volumes, we unhesitatingly conclude that the solubility of carbon in Tc cannot exceed 17 at.%. In brief, the predicted Tc$_6$C has the largest C concentration.
Fig. 3 (a) Experimental curve of normalized EXAFS signal (solid line) and optimized theoretical curve (points), and (b) modulus of the Fourier transform for the experimental EXAFS spectrum (solid) and its optimized theoretical curve (circle points) for the Tc₅C sample with 50 at.% C (parameters of local structure are given in Table 1).

Table 1. Parameters of the local structure for the Tc₅C sample with 50 at. % C according to EXAFS data: coordination numbers N, interatomic distances R, and Debye–Waller parameters σ² (k = 3.0–16.6, R = 1.8–3.0 Å, ΔE = 17.0 eV, Rᵢ = 0.004)

<table>
<thead>
<tr>
<th>Sample</th>
<th>Scattering path</th>
<th>N</th>
<th>R, Å</th>
<th>σ², Å</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tc₅C</td>
<td>Tc-Tc</td>
<td>12</td>
<td>2.72</td>
<td>0.0057</td>
</tr>
</tbody>
</table>

High-temperature cubic phase of elemental technetium In the past, a high-temperature cubic phase was taken for NaCl-type TcC²⁶,²⁷, but this cubic phase was also proposed to be pure technetium in the light of NMR results³⁰,³¹. This long-standing puzzle, of great scientific and technological significance, could be solved with the help of the trend of stability of TM carbides. Namely, NaCl-type TcC cannot be the high-temperature cubic phase observed in experiments. The lattice of cubic Tc is different from the Tc sublattice of NaCl-type TcC (Fig.4), due to significant lattice expansion caused by C interstitials of TcC. And thus, their XRD spectra should be different. To prove this conclusion, we simulated the XRD spectra of cubic Tc and NaCl-type TcC. The main peak of cubic Tc locates at 2θ =40° (with
X-ray wavelength 1.540562 Å), which is the same as the experimental result (Fig.4a) 
25. However, the XRD spectrum of TcC deviates from the experimental observation, 
having the main peak at 2θ=36°. Once again, we demonstrate that Tc rather than TcC, 
accords with the high-temperature cubic phase obtained in experiments 25-27.

Fig.4 Simulated X-ray diffraction (XRD) spectra for (a) cubic Tc and (b) NaCl-type TcC with the 
x-ray wavelength of 1.540562 Å. In (a), we illustrate the experimental XRD of Tc metal annealed 
with 50 at.% C 25.

Of course, our calculation predicts that at high temperature the cubic structure 
will be elemental technetium. This can be directly checked, and we performed 
quasiharmonic free energy calculations to investigate relative stability of the fcc and 
room-temperature hexagonal (hcp) forms of technetium. Above 1775 K, cubic (fcc) 
Tc is more stable than the hcp phase of Tc (Fig.5), due to its larger vibration entropy.
This result roughly agrees with an experimental conclusion that the cubic phase is 
stable above 1835 °C (2108 K) 26, in which the deviation of transition temperature 
may be caused by disordered interstitial carbon atoms. Their concentration (x) can be 
roughly estimated through considering the $E_{C-dis}$ of fcc-Tc and contribution of 
configurational entropy, i.e., $RT[x\ln x+(1-x)\ln(1-x)]$. Even at 2000 K, the 
concentration of disordered carbon is in the region of 7.67 at.%< $x$< 11.1 at.%. To sum 
up, Tc rather than TcC, is the observed high-temperature cubic phase 26, 27.
Discussions

Trends of stability for TM carbides can be easily rationalized, as we have shown above. With increasing filling of the d-band, TM-C bonds become weaker and weaker from left to right of the Periodic Table for 3d, 4d and 5d TM series. This diminishes the thermodynamic driving force for incorporation of C atoms in the TMs lattice; Tc corresponds to the break point, with easy carbide formation to its left and no carbide formation to its right. This rule easily explains why such compounds as TcC \(^{29, 41}\) and OsC \(^{4}\) are impossible. Formation of multiphase assemblages often obscures analysis. For example, a multiphase of Mo carbides was synthesized, as low-cost catalysts for hydrogen evolution reactions \(^{9}\). As reported \(^{13}\), many TM\(_x\)C\(_y\) compounds may remain unidentified, but recent theoretical discoveries of such compounds \(^{6, 14, 15}\) suggest that state-of-art theoretical approaches will play an increasingly important role in further discovery of TM\(_x\)C\(_y\) compounds, and such discoveries can be greatly aided by simple trends, such as the one discussed here.

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A simple understanding on the trend of stability for transition metal carbides